

Приложение 3.

$$a = 1.$$

1) Таблица №1.

$$\int 0 \cdot dk = c; \int_{a=1}^b 0 \cdot dk = c(b-a) = c(b-1)$$

| | | | | | | | | | | | | |
|-------|---|----|----|----|----|----|----|----|----|-----|-----|-------------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | ... | k |
| y_k | C | 2C | 3C | 4C | 5C | 6C | 7C | 8C | 9C | 10C | ... | $k \cdot a$ |

2) Таблица №2.

$$C_{k-1}^1 = k-1; \int_a^b (k-1)dk = 0,5(b^2 - 2ab + 1); y_k = y_{b-1} = 0,5 + 1,5C_{k-1}^1 + C_{k-1}^2$$

| | | | | | | | | | | | | |
|-------|-----|-----|-----|-----|------|------|------|------|------|----|-----|-------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | ... | k |
| y_k | 0,5 | 2,0 | 4,5 | 8,0 | 12,5 | 18,0 | 24,5 | 32,0 | 40,5 | 50 | ... | y_k |

3) Таблица №3.

$$C_{k-1}^2 = 0,5(k^2 - 3k + 2); \int_1^b C_{k-1}^2 dk = 0,5 \int_1^b (k^2 - 3k + 2)dk = 0,5(\frac{1}{3}b^3 - 1,5b^2 + 2b - 0,83333...);$$

$$y_k = y_{b-1} = -0,08333... + 0,41666...C_{k-1}^1 + 1,5C_{k-1}^2 + C_{k-1}^3$$

| | | | | | |
|-------|-------------|-------------|-----------|-----------|-------------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 |
| y_k | -0,08333... | 0.3333... | 2,25 | 6,6666... | 14,58333... |
| $b-1$ | 6 | 7 | 8 | 9 | 10 |
| y_k | 27,000 | 44,91666... | 69,333... | 101,25 | 141,666... |

4) Таблица №4.

$$C_{k-1}^3 = \frac{1}{6}(k^3 - 6k^2 + 11k - 6);$$

$$\int_1^b C_{k-1}^3 dk = \frac{1}{6} \int_1^b (k^3 - 6k^2 + 11k - 6)dk = \frac{1}{6}(0,25b^4 - 2b^3 + 5,5b^2 - 6b + 2,25); b-1 = k$$

$$y_k = y_{b-1} = -0,041666... - 0,041666...C_{k-1}^1 + 0,41666C_{k-1}^2 + 1,5C_{k-1}^3 + C_{k-1}^4$$

| | | | | | |
|-------|-------------|--------------|-------|----------|------------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 |
| y_k | 0,041666... | 0 | 0,375 | 2,666... | 9,375 |
| $b-1$ | 6 | 7 | 8 | 9 | 10 |
| y_k | 24 | 51,041666... | 96 | 161,375 | 266,666... |

5) Таблица №5.

$$C_{k-1}^4 = \frac{1}{24}(k^4 - 10k^3 + 35k^2 - 50k + 24)$$

$$\int_1^b C_{k-1}^4 dk = \frac{1}{24} \int_1^b (k^4 - 10k^3 + 35k^2 - 50k + 24) dk = \frac{1}{24}(0,2b^5 - 2,5b^4 + 11,666...b^3 - 25b^2 + 24b - 8,366...)$$

$$b-1 = k$$

$$y_k = y_{b-1} = -0,0263888... + 0,0152777...C_{k-1}^1 - 0,041666...C_{k-1}^2 + 0,41666...C_{k-1}^3 + 1,5C_{k-1}^4 + C_{k-1}^5$$

| | | | | | |
|-------|---------------|----------------|------------|-----------|--------------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 |
| y_k | -0,0263888... | -0,011111... | -0,0375 | 0,3111... | 2,9513888... |
| $b-1$ | 6 | 7 | 8 | 9 | 10 |
| y_k | 12,3 | 36,27361111... | 87,2888... | 183,2625 | 348,6111... |

6) Таблица №6.

$$C_{k-1}^5 = \frac{1}{120}(k^5 - 15k^4 + 85k^3 - 225k^2 + 274k - 120)$$

$$\int_1^b C_{k-1}^5 dk = \frac{1}{120} \int_1^b (k^5 - 15k^4 + 85k^3 - 225k^2 + 274k - 120) dk =$$

$$= \frac{1}{120} \left(\frac{1}{6}b^6 - 3b^5 + 21,25b^4 - 75b^3 + 137b^2 - 120b - 39,58333... \right)$$

$$b-1 = k$$

$$y_k = y_{b-1} = -0,64097222... - 0,00763888...C_{k-1}^1 + 0,0152777...C_{k-1}^2 - 0,041666...C_{k-1}^3 + 0,41666...C_{k-1}^4 + 1,5C_{k-1}^5 + C_{k-1}^6$$

| | | | | | |
|-------|----------------|----------------|----------------|-----------------|-----------------|
| $b-1$ | 1 | 2 | 3 | 4 | 5 |
| y_k | -0,64097222... | -0,6486111... | -0,64097222... | -0,6597222... | -0,329861111... |
| $b-1$ | 6 | 7 | 8 | 9 | 10 |
| y_k | 2,6402777... | 14,95902777... | 51,2513888... | 138,55902777... | 321,8402777... |

7) Таблица №7.

$$C_{k-1}^6 = \frac{1}{720}(k^6 - 21k^5 + 175k^4 - 735k^3 + 1624k^2 - 1764k + 720)$$

$$\int_1^b C_{k-1}^6 dk = \frac{1}{720} \int_1^b (k^6 - 21k^5 + 175k^4 - 735k^3 + 1624k^2 - 1764k + 720) dk =$$

$$= \frac{1}{720} \left(\frac{1}{7}b^7 - 3,5b^6 + 35b^5 - 183,75b^4 + 541,333...b^3 - 882b^2 + 720b - 227,02619... \right)$$

$$b-1 = k$$

$$y_k = -0,01426917989418 + 0,00448082010582C_{k-1}^1 - 0,00763888...C_{k-1}^2 + 0,0152777...C_{k-1}^3 -$$

$$-0,041666...C_{k-1}^4 + 0,41666...C_{k-1}^5 + 1,5C_{k-1}^6 + C_{k-1}^7$$

| | | | |
|-------|---------------------|--------------------|------------------------|
| $b-1$ | 1 | 2 | 3 |
| y_k | -0,01426917989418 | -0,00978835978836 | -0,012946428571428 |
| $b-1$ | 4 | 5 | 6 |
| y_k | -0,008465608465 | -0,0227347883359 | 0,292857142857142 |
| $b-1$ | 7 | 8 | 9 |
| y_k | 3,578587962962 | 19,183068783068783 | 71,0799107142857146666 |
| $b-1$ | 10 | | |
| y_k | 210,284391534391534 | | |

8) Таблица №8.

$$C_{k-1}^7 = \frac{1}{5040}(k^7 - 28k^6 + 322k^5 - 1960k^4 + 6769k^3 - 13132k^2 + 13068k - 5040)$$

$$\int_1^b C_{k-1}^7 dk = \frac{1}{5040} \int_1^b (k^7 - 28k^6 + 322k^5 - 1960k^4 + 6769k^3 - 13132k^2 + 13068k - 5040) dk =$$

$$= \frac{1}{5040} \left(\frac{1}{8}b^8 - 4b^7 + 53,666...b^6 - 392b^5 + 1692,25b^4 - 4377,333...b^3 + 6534b^2 - 5040b + 1533,291666... \right)$$

$$b-1 = k$$

$$y_k = -0,597081679894179894 - 0,00290178571428571C_{k-1}^1 + 0,004480820105820105C_{k-1}^2 -$$

$$-0,00763888...C_{k-1}^3 + 0,0152777...C_{k-1}^4 - 0,0416666...C_{k-1}^5 + 0,416666...C_{k-1}^6 + 1,5C_{k-1}^7 + C_{k-1}^8$$

| | | |
|-------|--------------------------|-----------------------|
| $b-1$ | 1 | 2 |
| y_k | -0,597081679894179894 | -0,599983465608465608 |
| $b-1$ | 3 | 4 |
| y_k | -0,598404431216931216931 | -0,599983465608465608 |
| $b-1$ | 5 | 6 |
| y_k | -0,597081679894179894 | -0,608449074074 |
| $b-1$ | 7 | 8 |
| y_k | -0,304224537037037 | 3.285730820105820105 |
| $b-1$ | 9 | 10 |
| y_k | 22,480166997354497347 | 93,571445105820105820 |

9) Таблица №9.

$$C_{k-1}^8 = \frac{1}{40320}(k^8 - 36k^7 + 546k^6 - 4536k^5 + 22449k^4 - 67284k^3 + 118124k^2 - 109584k + 40320)$$

$$\begin{aligned} \int_1^b C_{k-1}^8 dk &= \frac{1}{40320} \int_1^b (k^8 - 36k^7 + 546k^6 - 4536k^5 + 22449k^4 - 67284k^3 + 118124k^2 - 109584k + 40320) dk = \\ &= \frac{1}{40320} \left(\frac{1}{9} b^9 - 4,5b^8 + 78b^7 - 756b^6 + 4489,8b^5 - 16821b^4 + 39374,666..b^3 - 54792b^2 - 40320b - \right. \\ &\left. -11889,0777... \right) \end{aligned}$$